
Time Series

Applications to Finance

Ngai Hang Chan



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Time Series
Applications to Finance

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Chinese University of Hong Kong

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